

Summary of the onCALCULATION methods used in dbSEABED

Chris Jenkins

Institute of Arctic & Alpine Research (INSTAAR),
University of Colorado at Boulder,
Boulder CO, 80309-0450

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The module onCALCULATE performs a small amount of modeling to extend the outputs of dbSEABED to reasonable estimates of seafloor properties. This is particularly useful for geoacoustic and other physical properties which have no practical mappable data distribution based on actual analyses. The modeling is based on theoretical or empirical relations that are documented below. The chosen relationships may be replaced by others in the future as further physical properties research is published and as validation of the onCALCULATION results is done. Users of dbSEABED may choose whether to use these lower accuracy estimates in mappings or to work with map data coverages that are less reliable because they contain less data.

A couple of principles have guided the selection of relationships and their implementation: (a) that the methods should be transparent and well-documented, not complex, (b) they may be built on extracted or parsed parameter inputs, but not on values that are themselves onCALCULATED, (c) they might apply only to certain sections of the input parameter range, (d) they preferably are published relationships, but if not then (e) should be supported by the analysis of a substantial amount of data from a wide range of sediments.

The methods that are currently implemented are:

1. Grain size / Sorting from Gravel:Sand:Silt:Clay and Gravel:Sand:Mud Ratios

Gvl:Snd:Slt:Cly and Gvl:Snd:Mud (GSSC, GSM) ratios are in effect short grain size-fraction histograms for the sediments. An estimate of AV and SD grain size can be made from them as follows. Each class is assigned a central grain size value based on examinations of large USGS and other datasets in EXCEL. These GSSC(M) class central values result: -3, 2, 5, 7, (8) in phi.

A weighted mean and weighted standard deviation are formed across the GSSC or GSM classes, leading to an estimate of the average grain size and sorting of the sediment. A method of validation and uncertainty calculation is available by comparison of the results for samples where a mean/sorting is already measured.

2. Hydrographic Chart Bottom Type code

This code, described in UKHO (2005) and NOS (1997), has the form "Cy.S.Co". It is essentially the same as the US NOS codes. The calculation is mostly a matter of assigning textural classes in front-significant order based on the GSSC(M) ratios, but also with special classes "R", "Wd" where rock and weed memberships are significant. Thus, the output codes are minimal codes.

3. Folk and Shepard Classifications

These have been implemented following the schemes in Poppe and Polloni (2000).

4. P-wave Velocities for Consolidated Materials Based on Time-Average Model

This calculation is performed only where there is an indication of cementation or consolidation in the material, usually expressed by measured or parsed Shear Strength >50 kPa or porosity <35%, and where the porosity has been measured. Then:

$$mVp = (1 - \text{Poros}) / \text{VelSol} + \text{Poros} / \text{VelFlu}$$

where Poros is the fractional porosity of the material and VelSol and VelFlu are the solid and fluid phase p-wave velocities. The constants are: VelSol = 5000, VelFlu = 1520 (these are measured values, different from those optimized for models such as Biot Theory; see Thorsos et al, (2001)). The relation is associated with data over the whole range of porosities (Fig. 1). The time average model is attributed to Wyllie, et al, (1963).

Fig. 1. The distribution of sediments by their Porosity and P- and S-wave Velocity values. Several separate populations are apparent. For P-wave velocities, the loose sediments with low velocities from 34% porosity and following the Gassman function; consolidated sediments following the Time-average relation; apparently cemented sediments with anomalously high velocities for the porosity. The S-wave populations have yet to be explained.

5. Porosity Based on Mud Content of Loose Sediments

A compilation of many published analysis (Fig 2) results supports the empirical relationship:

$$m\text{Por} = 0.4 * \text{mud} + 43$$

for mud% > 7%. It appears to hold equally for terrigenous and carbonate sediments. Figure 3 illustrates the relationship for sediments of the Mississippi-Alabama-Florida (MAFLA) shelf.

Fig. 2. Empirical data supporting the Mud%-Porosity relation where mud fraction is >7%. The plotted data is a mix of terrigenous, carbonate, loose and consolidated samples, Mississippi-Alabama-Florida (MAFLA) shelf.

6. Porosity Based on Average Grain size

Richardson and Briggs (1993) proposed a relationship between porosity and average grain size (AvGrsz, phi units) based on their measurements of muddy and sandy sediments. The relation is inverted for the on-calculation, and is applied only in the range AvGrsz > 0 phi:

$$\text{Por} = 26.92 + 5.92 * \text{AvGrsz}$$

The form is less accurate than methods where the percent of mud is known, and is not used in those cases.

7. Coarse Fraction and the P-wave Velocity

Related to the porosity-mud fraction function is another between coarse fraction and Vp:

$$mVp = 0.0009 * \text{SpG}^3 + -0.14 * \text{SpG}^2 + 8.56 * \text{SpG} + 1512.76$$

where SpG is the percent coarse fraction. This polynomial is a poor fit and further work is required.

8. Wood-Gassman Equation for P-wave Velocity in Loose Sediments

This method of estimating Vp is applied to sediments with no evidence of consolidation. It depends on assumed values for some acoustic constants of the sediments: (a) the Bulk Moduli K for solid, fluid, frame (Ko1Sol, Ko1Flu and Ko1Fra 3.6E+10, 2E+09 and 4E+08, MKS units); and (b) the Rigidities for solids and frame (RigidSol, RigidFra 2.2E+07, 1E+07).

The sediment Bulk Modulus and Density are:

$$\text{Ko1} = (1-f\text{Por})/\text{Ko1Sol} + f\text{Por}/\text{Ko1Flu}$$

$$\text{SedDens} = (1-f\text{Por})*\text{DenSol} + f\text{Por}*\text{DensFlu}$$

And the p-wave velocity is calculated as:

$$\text{Qgass} = \frac{\text{Ko1Flu} * (\text{Ko1Sol} - \text{Ko1Fra})}{f\text{Por} * (\text{Ko1Sol} - \text{Ko1Flu})}$$

$$\text{Kgass} = \text{Ko1Sol} * (\text{Ko1Fra} + \text{Qgass}) / (\text{Ko1Sol} - \text{Qgass})$$

$$\text{VPgass} = \sqrt{(\text{Kgass} + 4/3 * \text{RigidFra}) / \text{SedDens}}$$

Gassman (1951). VPgass is output as the estimate of Vp.

The Wood-Gassman relation is one of several that have been proposed between porosity and the acoustic velocities. As can be seen on Fig. 1, the relation has an associated population of data ranging only between 35-80% porosity. In the dbSEABED on-calculation it is applied only where porosity is known and >35% and where there is no indication of consolidation.

9. Roughness from Grain Protrusion for Gravels and Coarser

Kirchner and others (1990) offer a method for the calculation of grain protrusion (PnKir) above a sediment surface:

$$\begin{aligned} \text{EnKir} &= 0.5 * (\text{DnKir} - \text{D50Kir} + (\text{DnKir} + \text{D50Kir}) * \cos(\text{F100nKir})) \\ \text{PnKir} &= \text{EnKir} + \pi * \text{D50Kir} / 12 \end{aligned}$$

where D50Kir and DnKir are the median and nth percentile grain sizes, and F100nKir is the Friction angle with a test grain of the 100-nth grain size percentile. In on-calculation the estimation is done only using the central and the coarsest grain sizes (CSESTsz; either PRS or EXT) for D50Kir and DnKir. PnKir is output as an estimate of roughness.

10. Roughness Metric from Outsized Clasts

This metric was employed as an early measure of seabed roughness; it is based on an idealized arrangement of the sediment clasts and particles. The coarsest grain size is logged from previous processing of grain size analysis and descriptive data inputs, or is estimated from the average plus 2 times the SD (sorting) where both are known. The vertical roughness is estimated as half the clast size (D) with allowance for natural oblateness:

$$dZ = 0.5 * D * \text{CSF}$$

where CSF is the Corey Shape Factor to account for non-sphericity. (In naturally worn materials CSF is about 0.7; e.g., Jimenez & Madsen 2003.) The spacing of the clast grain size is assessed as half the repeat distance implied by the fractional linear abundance P_L of the outsized clast with size D. Linear

abundance is related to areal and volume (most common) abundances P_A and P_V as: $P_L = P_A^{1/2}$,

$P_L = P_V^{1/3}$. The clast protrusion and half-spacing are output as the vertical and horizontal roughness scales.

11. Critical Shear Stress

If the material shows evidence of consolidation, then the Critical Shear Stress (CSS, N/m^2) is set equal to the reported Shear Strength (kPa). Whitehouse et al. (2000, p. 27) discuss the relationship, which is interim in the on-calculation.

For loose sediments, the functions related to grain size (AvGRZ) were investigated based on data from many studies (Fig. 3). This work was done in conjunction with IOW, in Germany. The conclusions were: (i) with fine grained loose sediments where density or porosity are known, use the relationship of Mitchener, et al, (1996, in Whitehouse, et al, (2000)); (ii) else for those sediments use a generalized value of 0.5 N/m^2 ; (iii) for loose coarse grained sediments use a log-linear relationship as shown in Fig. 3, $\log_{10}(\text{CSS}) = \log_{10}[1.04 - \text{AvGRZ} * 0.6]$.

Bioturbation and bioconsolidation were not recognized in the estimation process for fine sediments, though they can be important (see Black, et al, (2002)). A correction of minor importance compared to the overall uncertainties is applied in the on-calculation.

Fig. 3. A compilation of Critical Shear Stress results by sediment grain size over the gravel to clay range. Over 24

references were used referring to marine and river sediments, field and laboratory experiments, on unaltered and manipulated natural sediments.

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